



Quasi Stars

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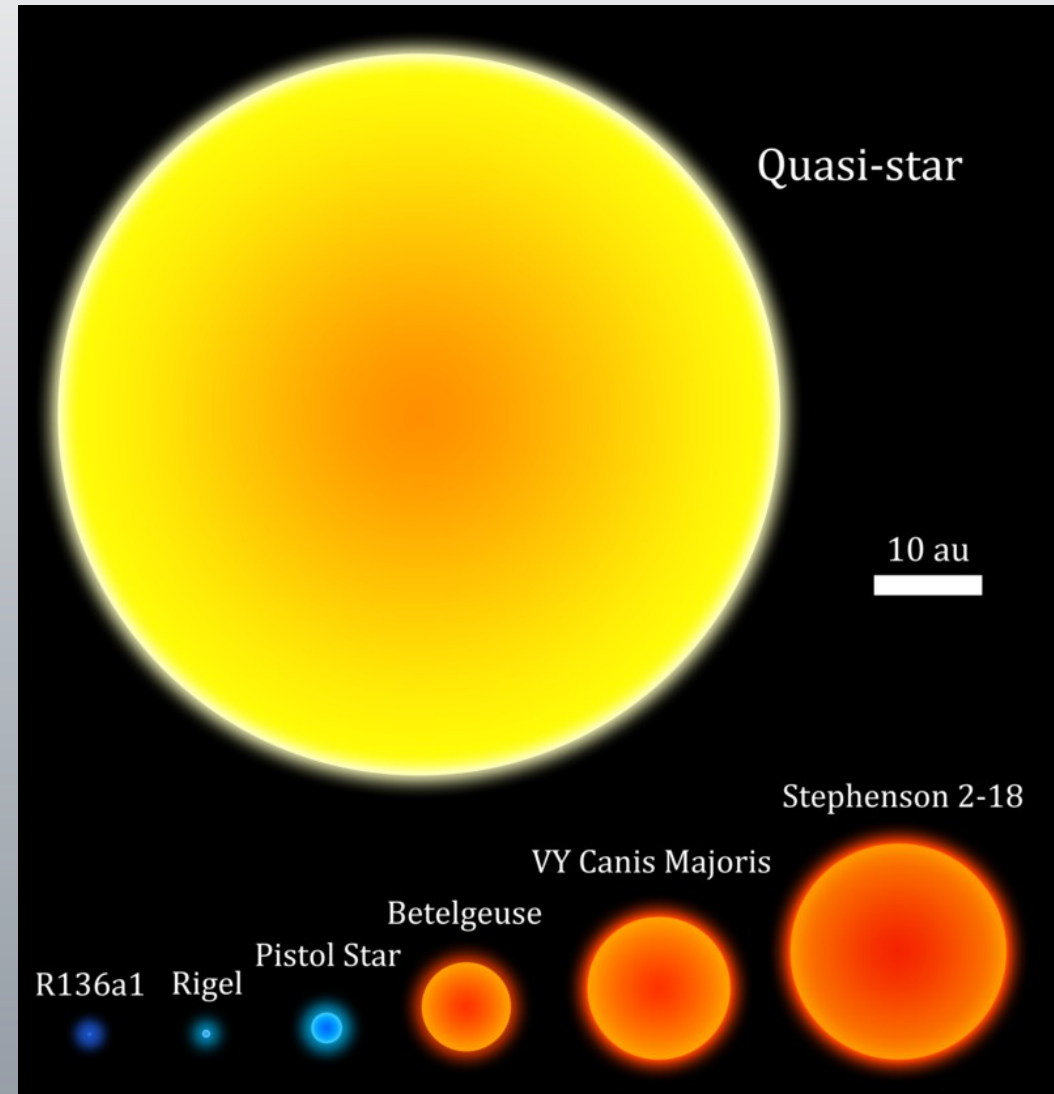
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- Definition of a Quasi-star
- General Quasi-star Model
- Analytic Model
- Numerical Model
- Co-Evolution Model
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Definition of a Quasi-star

- Quasi-star (hypothetical concept)
 - Extremely bright and massive star in the early universe
 - Unlike regular stars these were powered by a central black hole
- Quasi-star could be a solution for the SMBH problem
 - Why SMBH appear much earlier than traditional theories expect

=> Lets look into in more detail

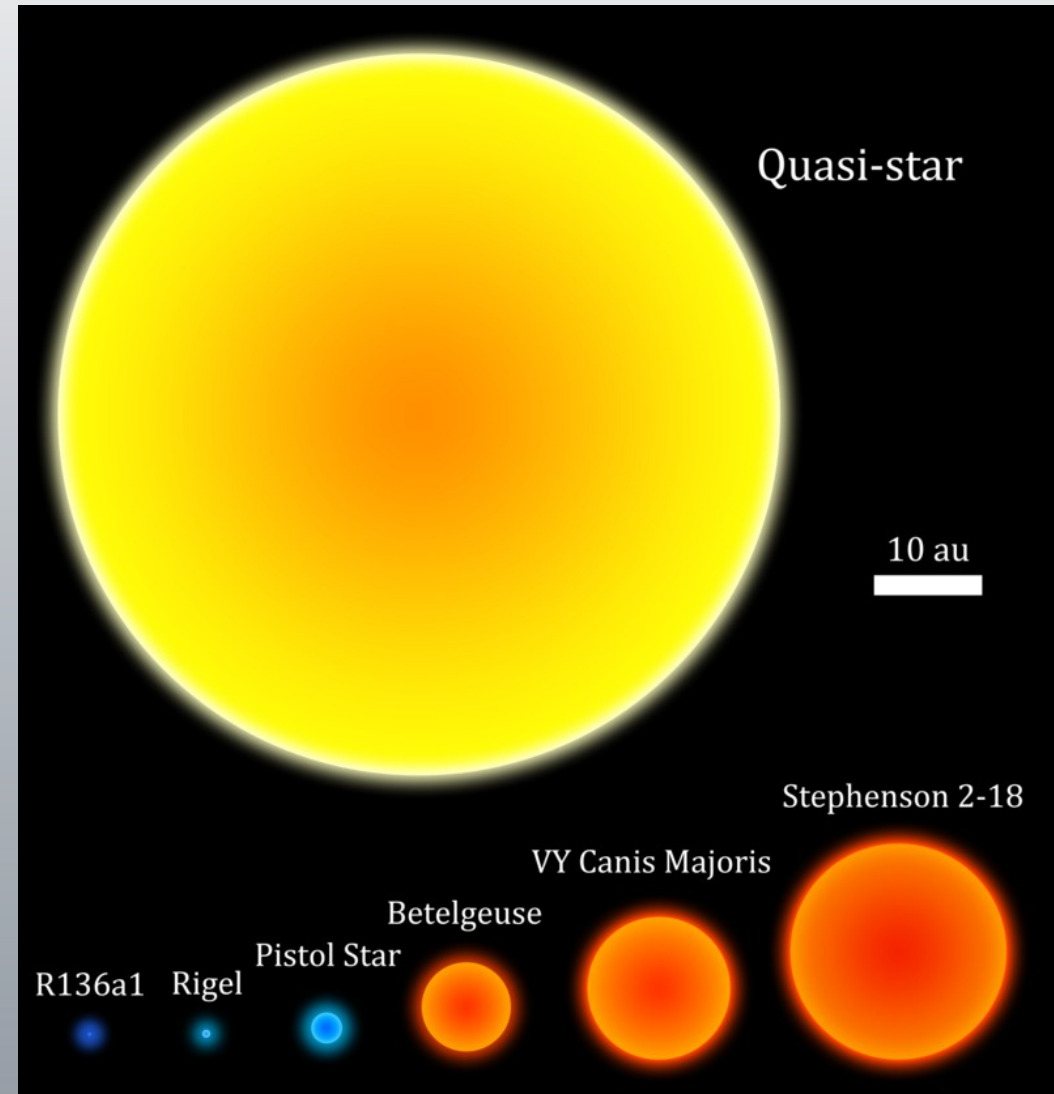


General Model

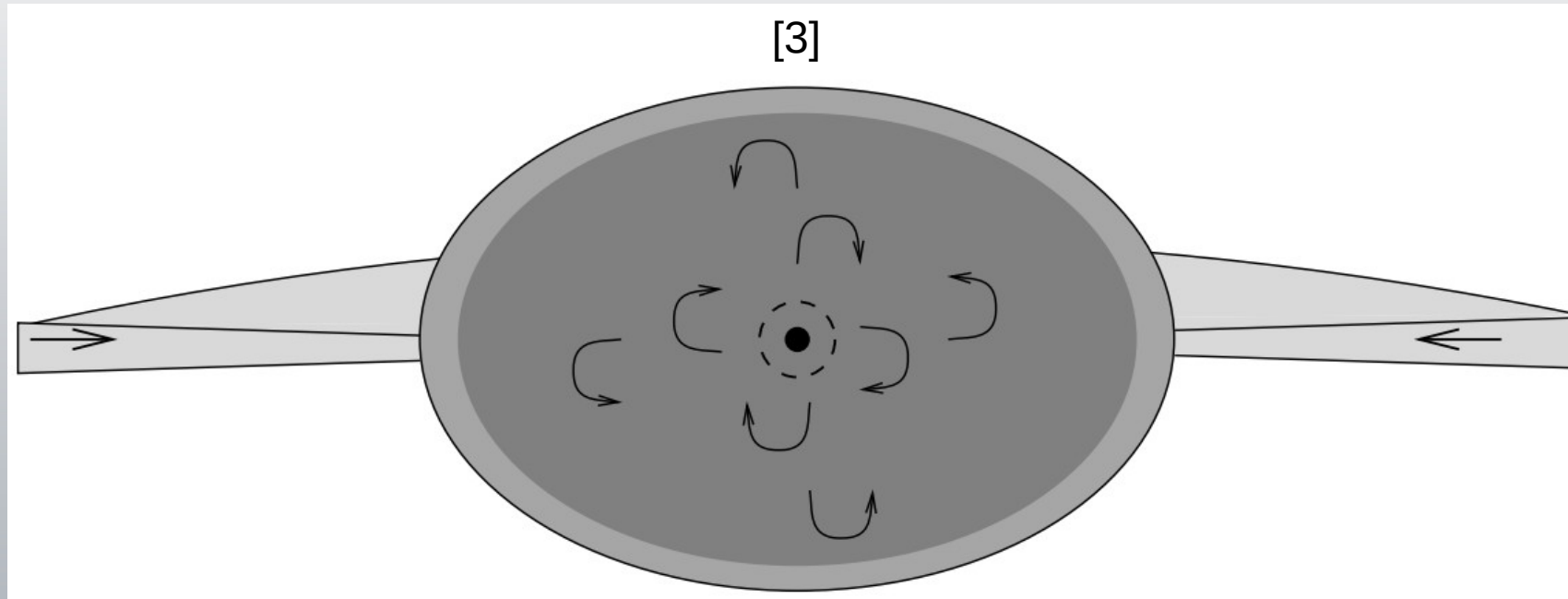
- Model of a quasi-star
- Calculated by Begelman, Rossi and Armitage
- To estimate
 - Maximum BH mass possible
 - Photospheric temperature
 - Photospheric luminosity

=> So that next-generation observatories could find such objects

=> Lets look at the general features of the quasi star in this model



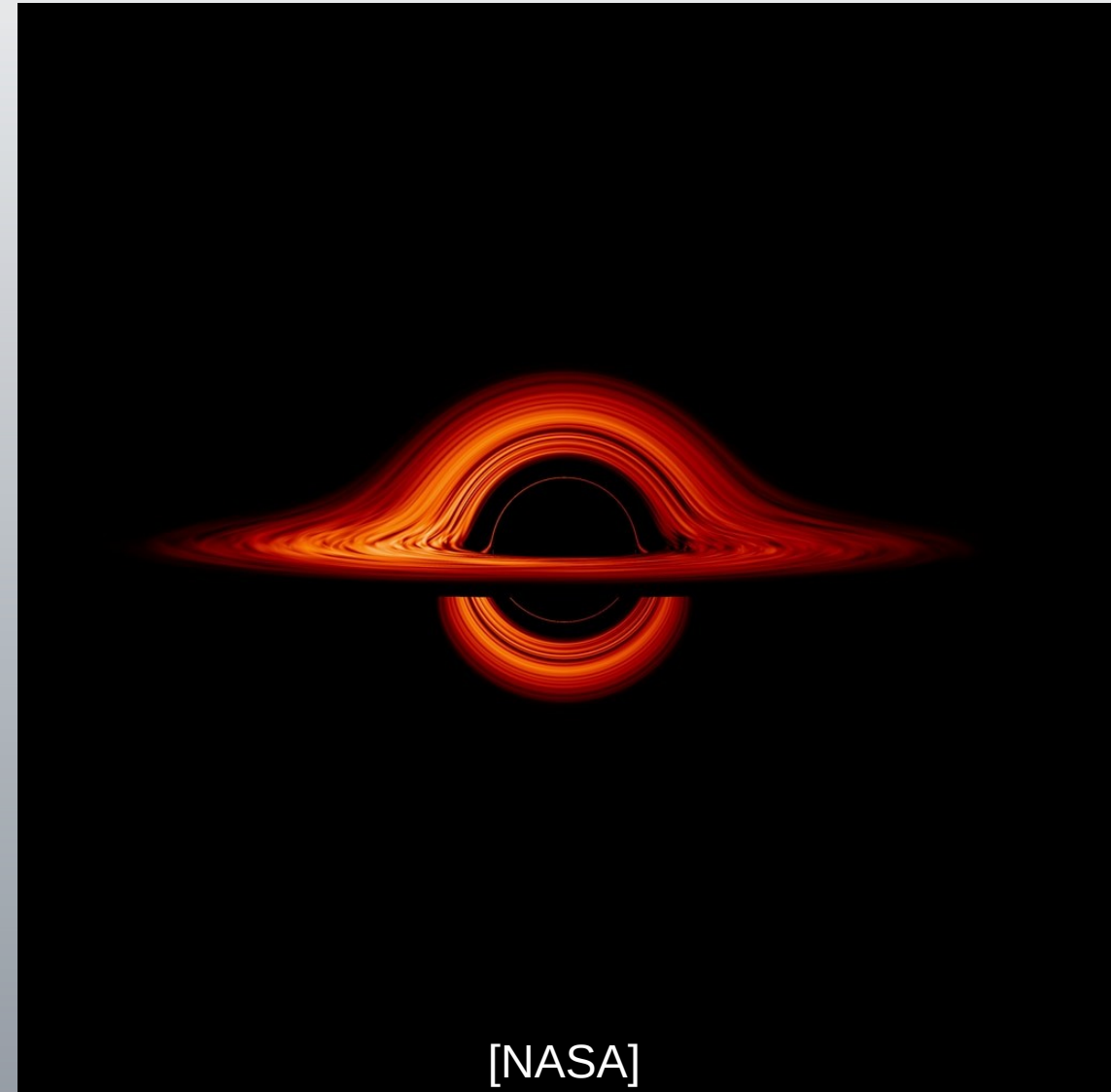
General Model



- Spherically symmetric Pop. III star
- Created in the very early Universe
- Made out of pristine gases
- Unlike today's star
 - No metal pollution
 - With on-going disc accretion
- Creation of central black hole (dot)
 - Black hole grows from the envelope
- Limited by the Eddington luminosity
 - Maximum Luminosity of a stable radiating object

General Model

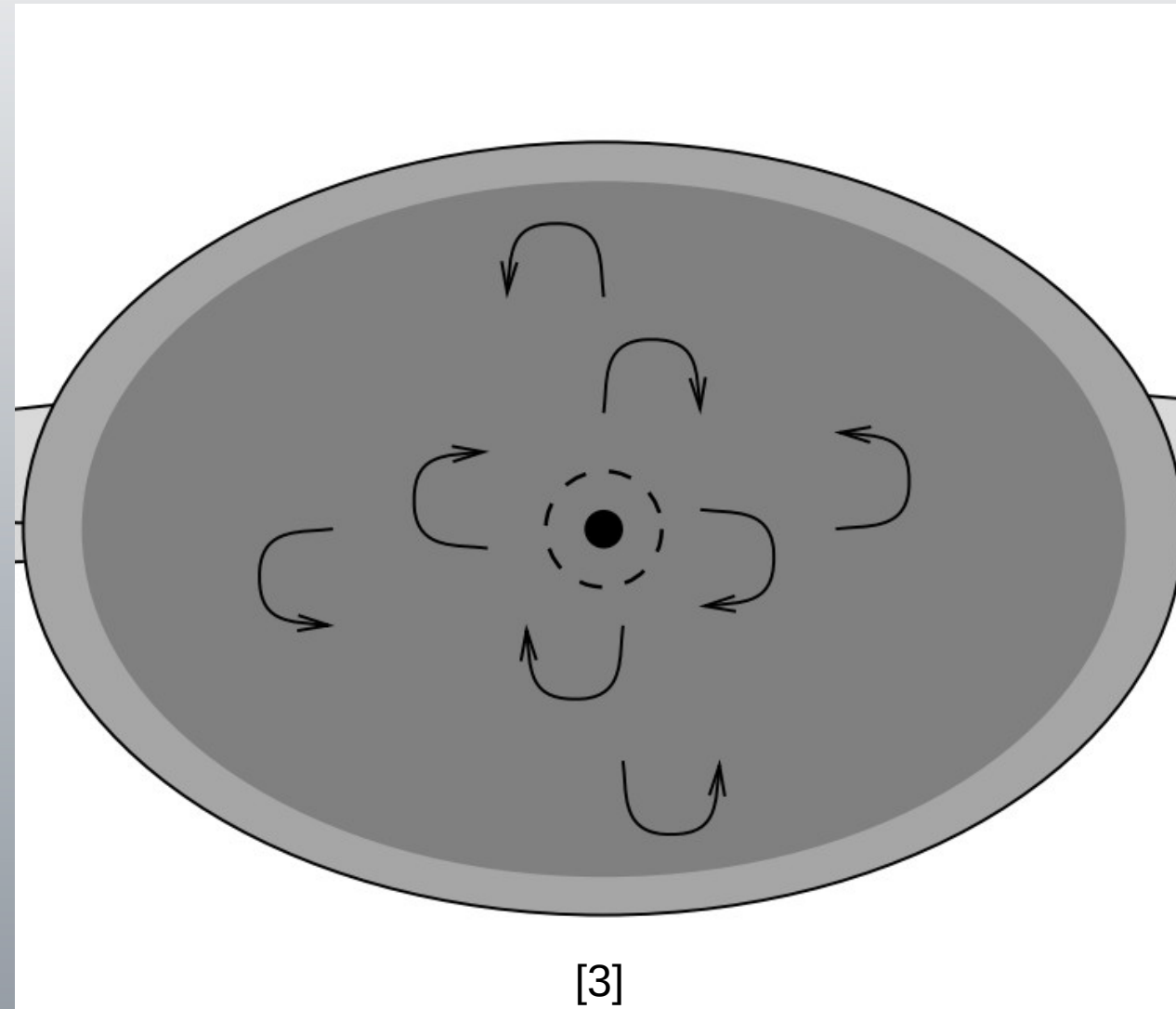
- The quasi-stars accretion rate will be limited by the Eddington luminosity for the stars total mass
- Accretion rate
 - Massive object attracts mass
 - Accretion disc can form
- Super-Eddington luminosities
 - Radiation dominates Gravity
 - Blowing the envelope away



General Model

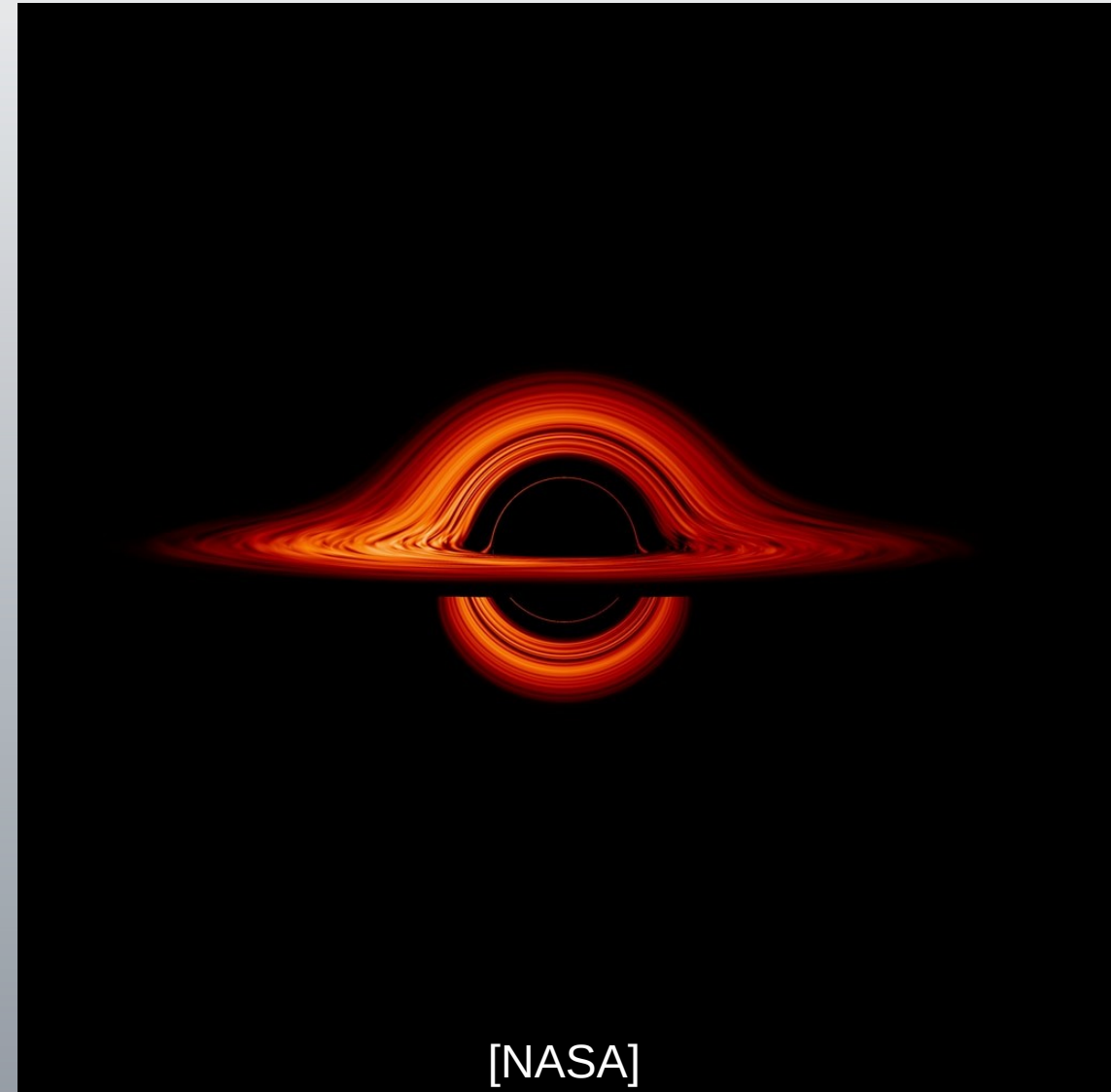
- Assuming hydrostatic equilibrium
 - Not exceed the Eddington Limit
- The Black holes luminosity
 - Convectively transported through the central zone of the envelope (dark grey) to the transition zone
 - Where convection becomes inefficient and radiation takes over
 - There the radiation zone (light grey) begins

=> Go to the analytical model



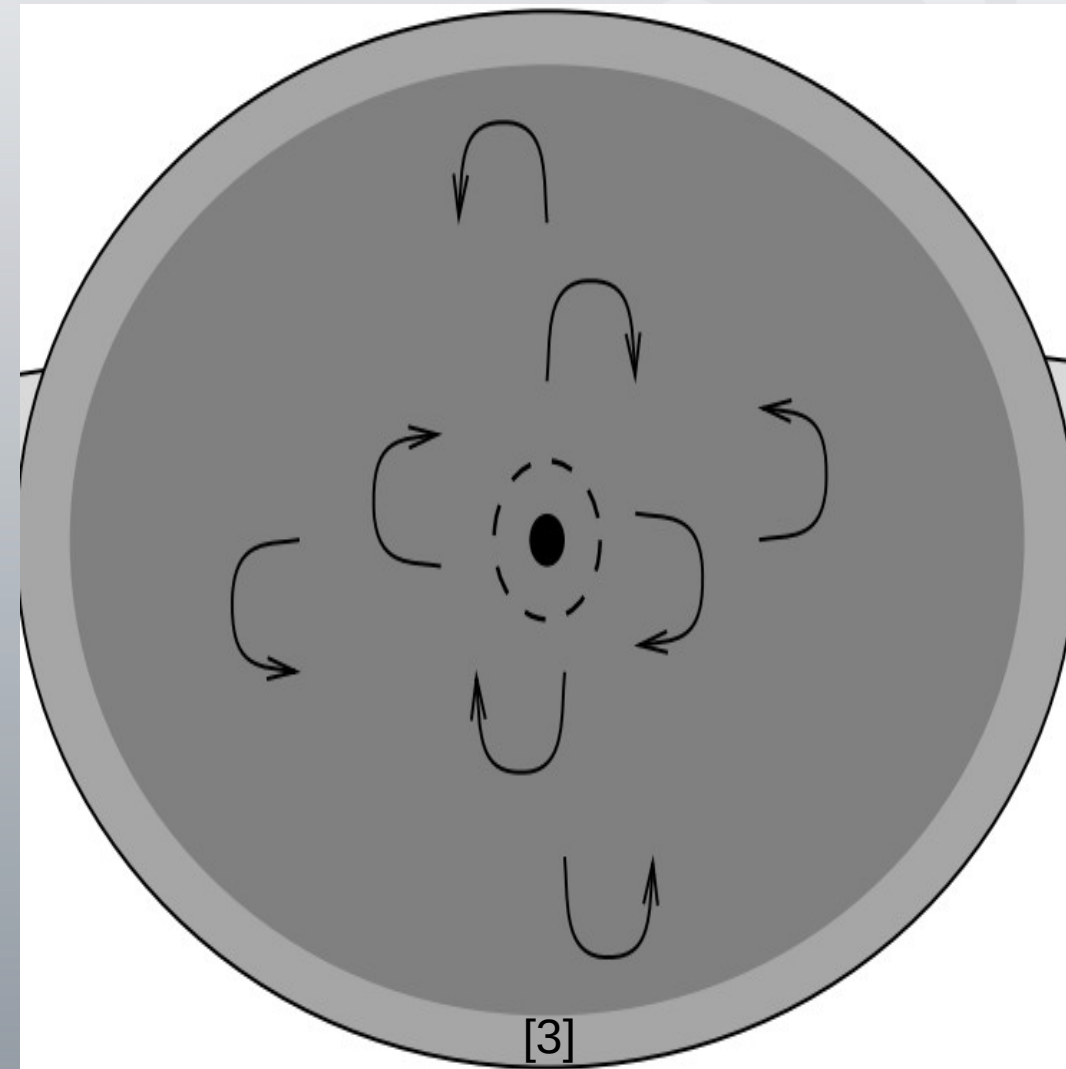
Analytic model

- The envelope mass $M_* \gg M_{\text{BH}}$
 - Spherically symmetric placed
 - Luminosity is exclusively generated by the BHs accretion disc
 - Fusion will be neglected
 - Black hole accretion is energetically much more efficient than fusion
 - Very small effect on the opacity
- => How does the inner region of the quasi star look like?



Analytic model

- Central regions of the envelope
 - Electron scattering opacity dominates
 - Envelopes mass $\geq 10^3 M_{\odot}$
 - Quasi-star envelopes are primarily supported by radiation pressure
 - Strongly convective
 - Can be described through $n = 3$ ($\gamma = 4/3$) polytropes
 - With uniform in density (ρ_c), pressure (p_c) and temperature (T_c)
- => Therefore the use of Bondi accretion is justified (similar boundary conditions)



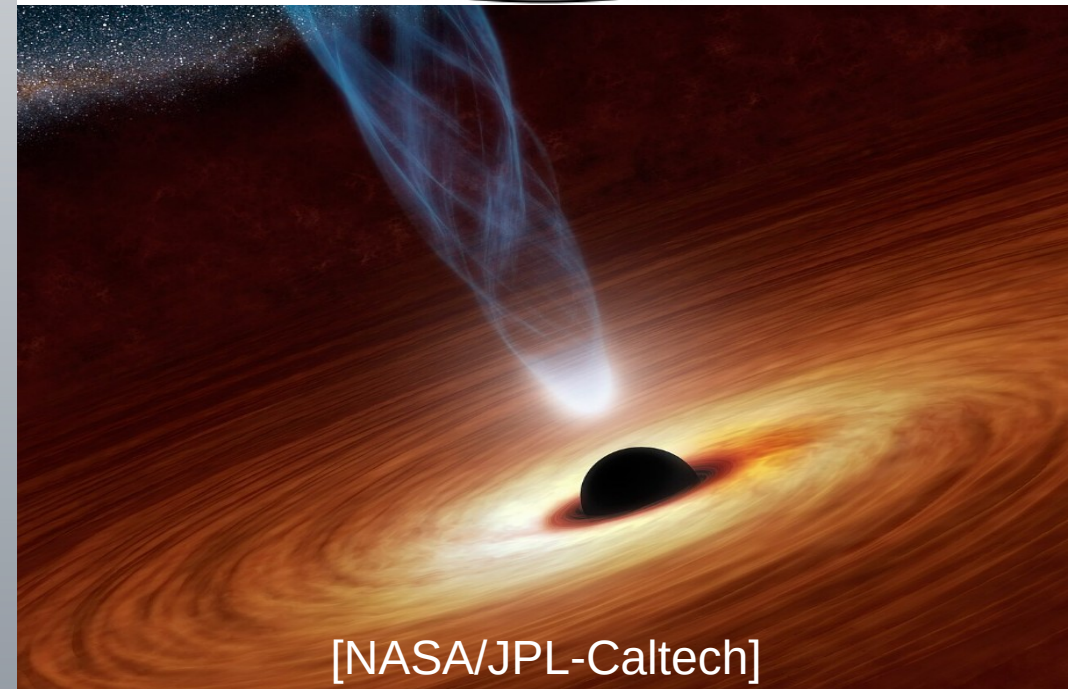
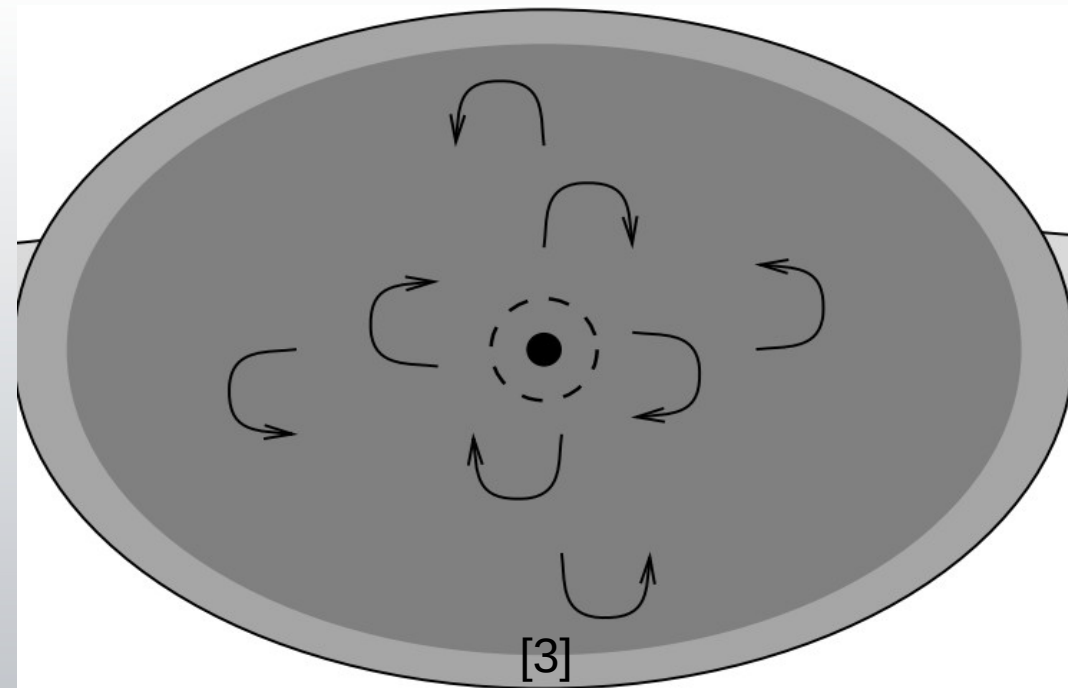
Analytic model

- Bondi accretion: Spherical accretion onto a compact object travelling through an interstellar Medium

$$\dot{M}_{Bo} = \frac{4 \pi (G M_{BH})^2 \rho_c}{(c_c^3 \sqrt{2})} \quad R_{Bo} = G \frac{M_{BH}}{c_c^2}$$

- Bondi Radius: The distance at which matter can be gravitationally captured (dotted line)
 - Absence of an efficient exhaust
 - Like jet or evacuated funnel
 - Energy must be transported beyond R_{Bo}

=>But only realistic in the complete absence of rotation



[NASA/JPL-Caltech]

Analytic model

- Thick accretion disc around the BH
- Where angular momentum transport is needed to create accretion

=> Efficiency of the BHs accretion disc will be modified by the parameter α

- The parameter $\alpha < 1$ accounts for energy sinks within the Bondi radius
- Inefficient convection, presence of outflows, etc.
- So any inefficiency of angular momentum transport

$$R_{Bo} = G \frac{M_{BH}}{c_c^2} \quad c_c = \left(\frac{4 p_c}{3 \rho_c} \right)^{1/2} \quad p_c = \frac{a T^4}{3}$$

$$\dot{M}_{Bo} = \frac{4 \pi (G M_{BH})^2 \rho_c}{(c_c^3 \sqrt{2})}$$

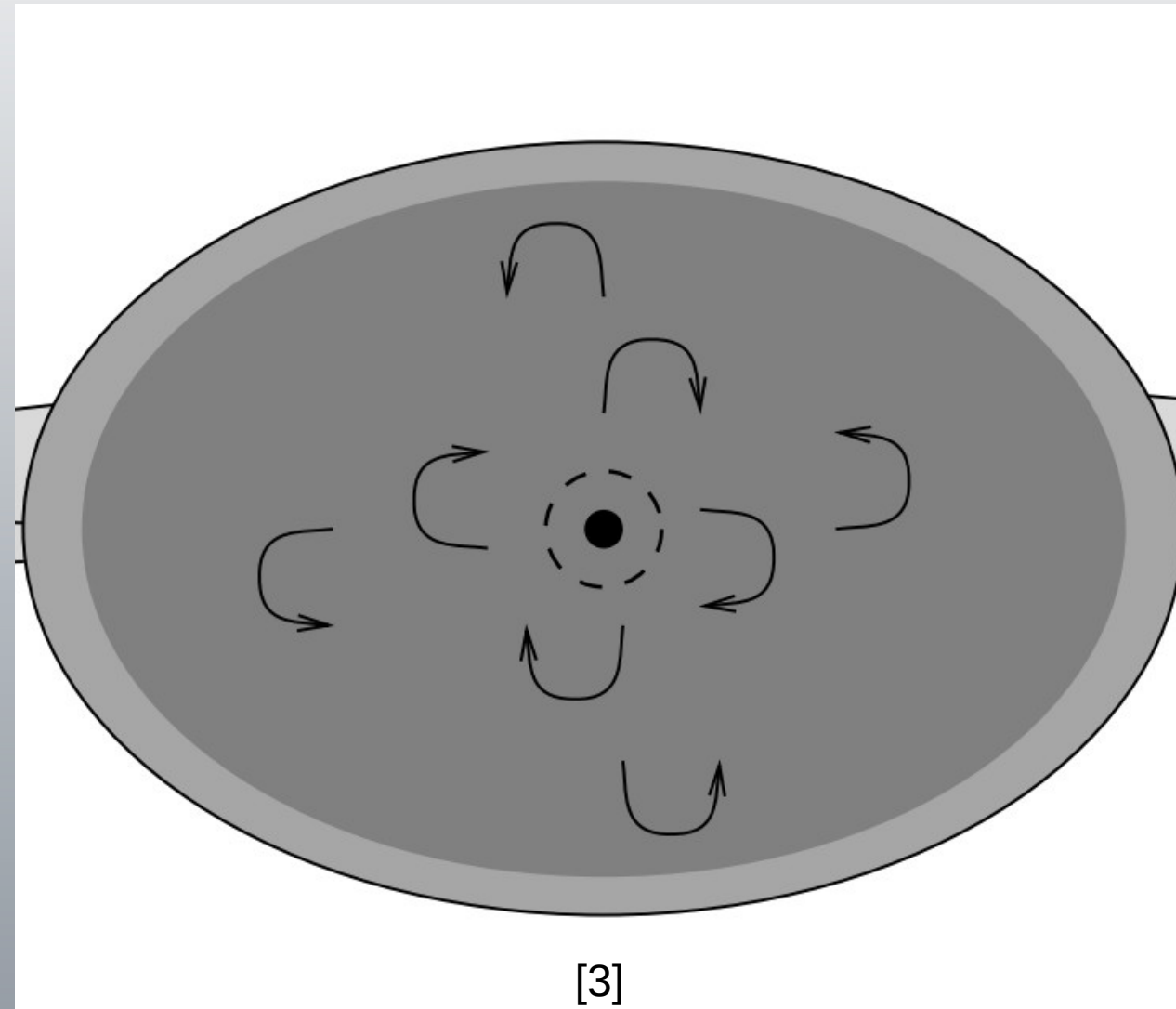
$$L_{BH} = \alpha \dot{M}_{BH} c^2 \quad \alpha \approx O(0.1)$$

$$L_{Bh} = 4 \pi G^2 \alpha M_{BH}^2 \rho_c^{3/2} p_c^{-1/2}$$

$$\rightarrow L_{Bh} = 6.6 \cdot 10^{42} \alpha m_{BH}^2 m_*^{-3/4} T_6^{5/2} \text{ erg s}^{-1}$$

Analytic model

- Expecting L_{BH} to be very close to the Eddington limit at the transition
 - Assuming the convective zone encompasses nearly the entire mass and radius of the envelope
- => Radius and mass of the radiative layer are negligible in comparison to the envelopes mass and radius
- => Estimates through polytropic relations: $R_{\text{quasi star}} \approx 10^2 - 10^3 \text{ au}$,
 $T_{\text{quasi star}} \approx O(10^3 \text{ K})$ and $T_{\text{ph}} \approx 10^3 \text{ K}$

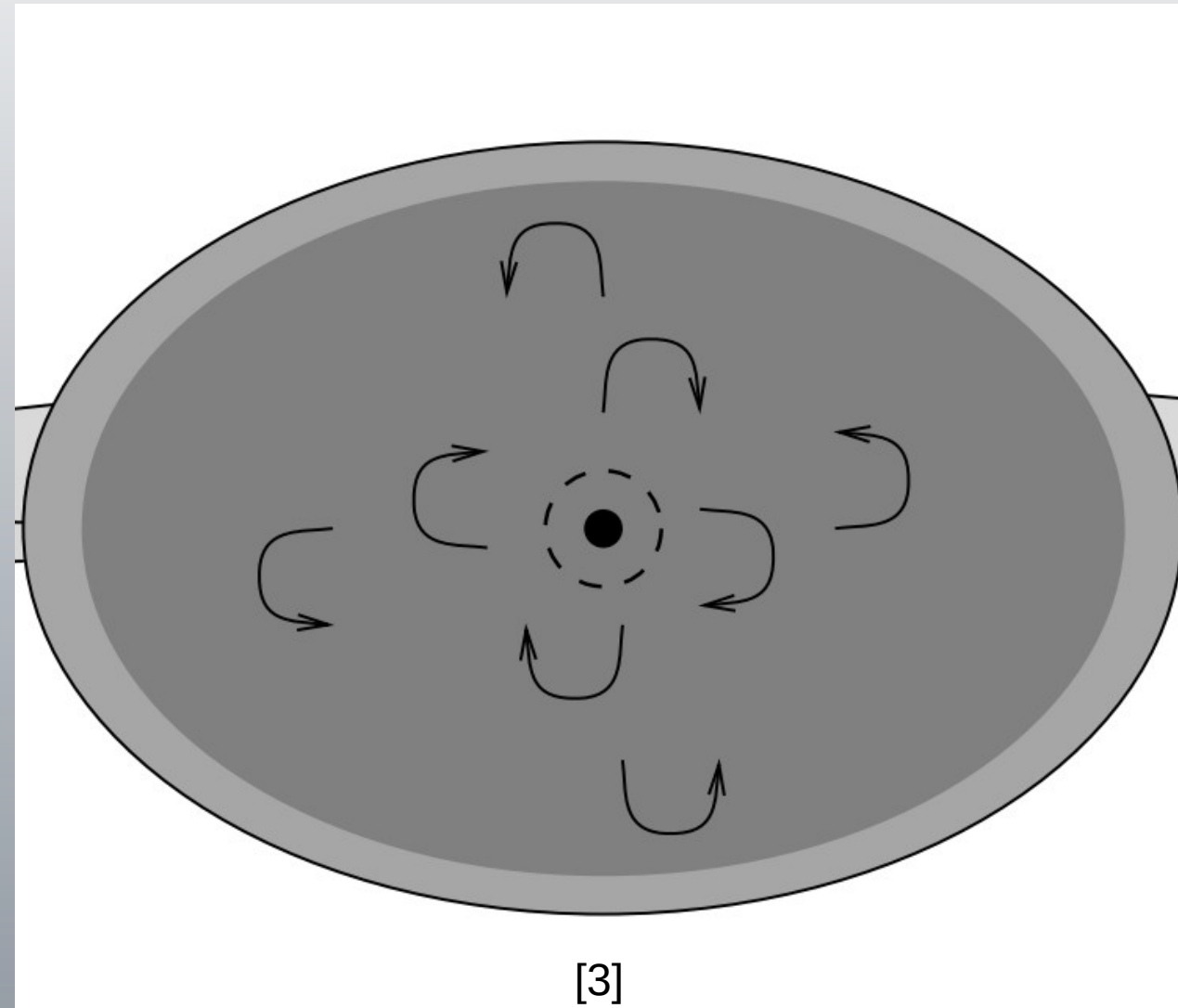


Analytic model

- Radiative layer (light grey)
- Opacity determines the layer structure of the layer
- Mainly electron scattering
- Metals would increase the opacity
- Opacity is based on Pop III opacity tables of Mayer & Duschl from 2005 (short: MD05)

$$\text{Fitting: } \kappa(T) = \frac{\kappa_0}{1 + (T/T_0)^s}$$

=> The opacity is only temperature dependent in this model

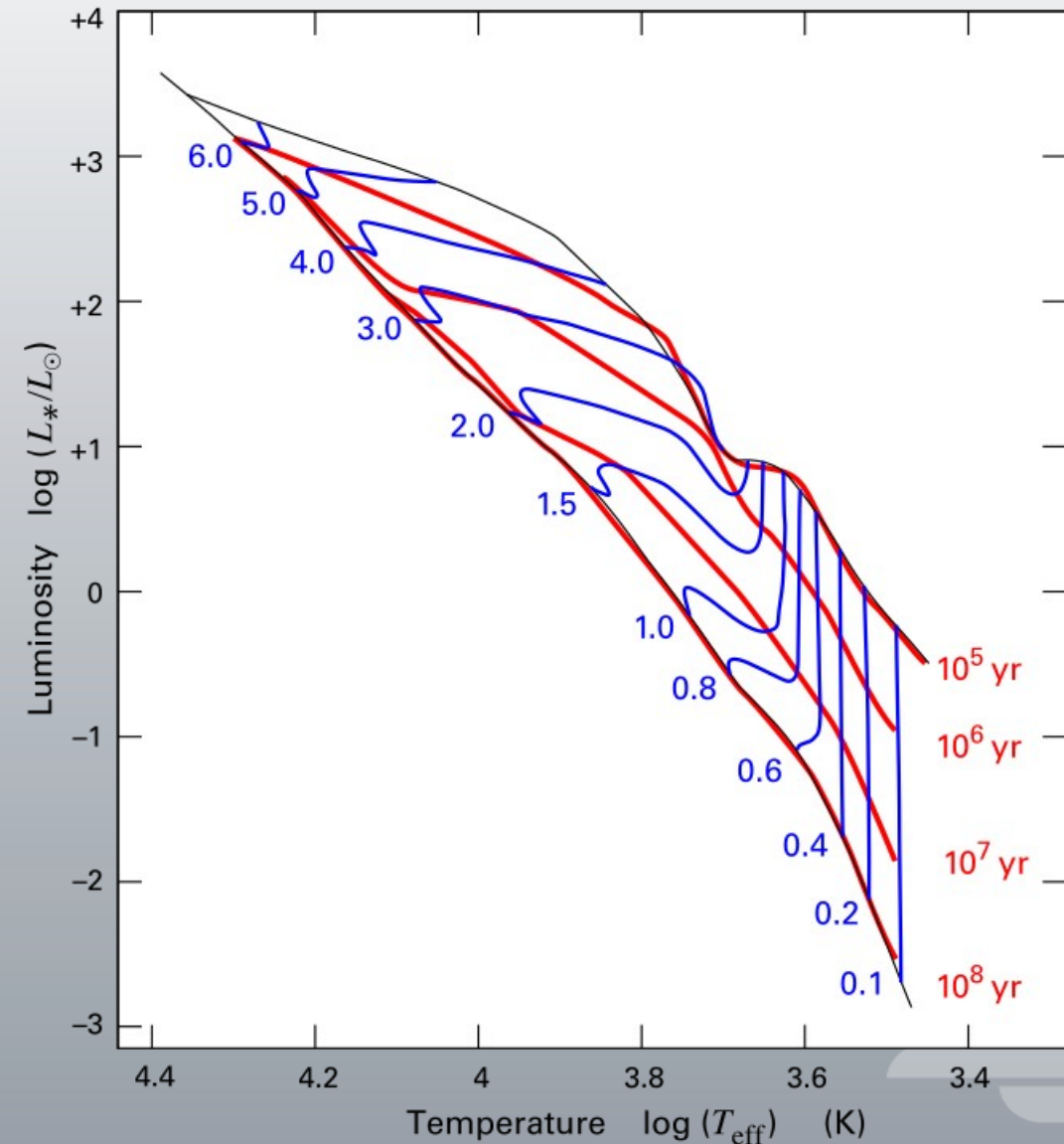


Analytic model

- Eddington factor l_{tr} at the transition radius
- Gravity to radiation pressure ratio
- Must be below 1 to avoid the dispersion of the quasi-star through building up pressure
- $l_{tr} < 1$ = hydrostatic equilibrium
- $l_{tr} > 1$ = Opacity crises

$$\Rightarrow T_{ph,min} \approx 4500K, T_{tr,min} \approx 55000K$$

- Analogous to the “Hayashi track“
- Limits the temperatures of red giants and convective protostars



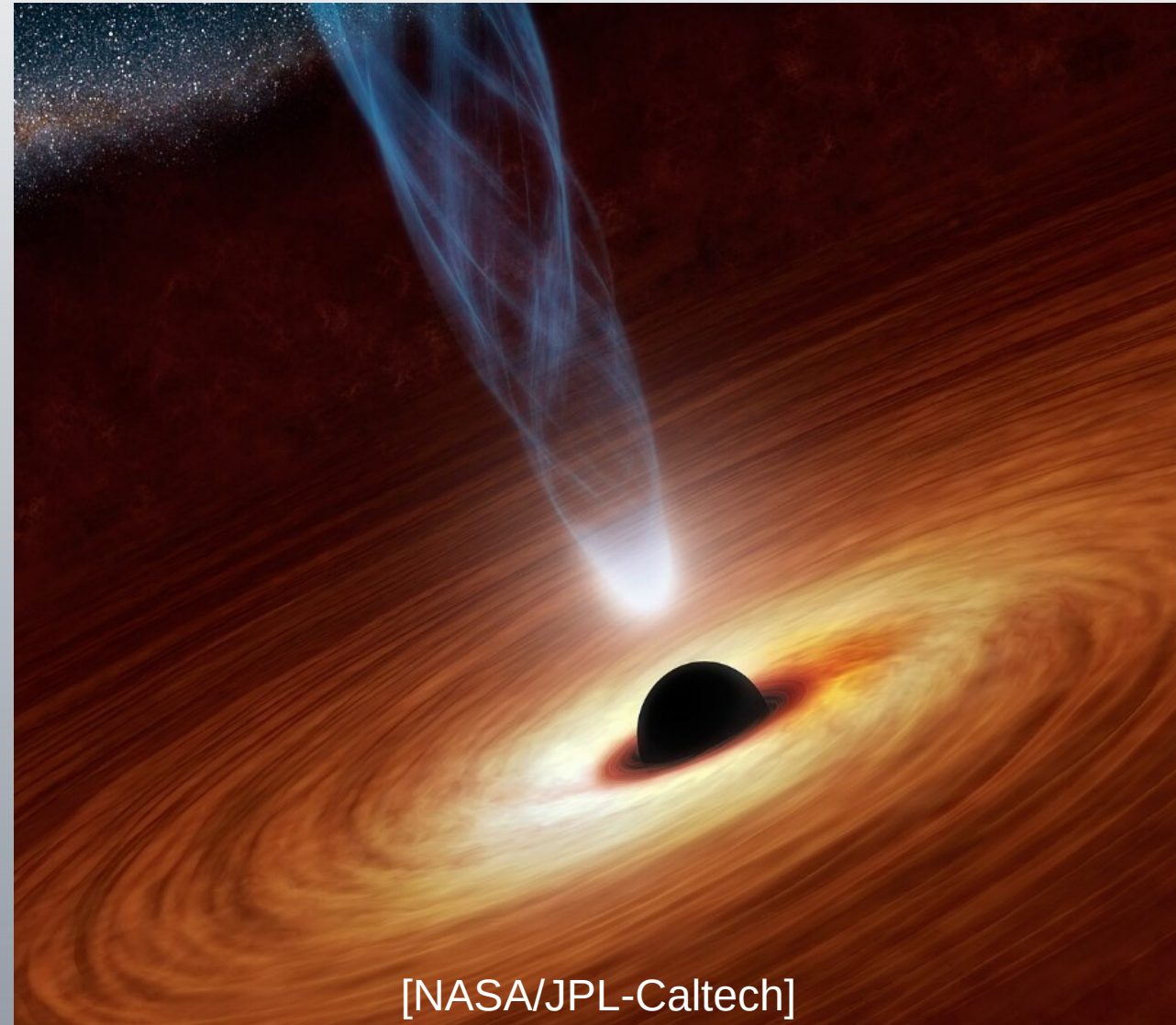
[The Formation of Stars]

Analytic model

- Analytic model
 - Decent estimate for certain features of the stars structure
 - Opacity ignores bound–free and free–free absorption at $T > 8 \cdot 10^3$ K
 - Pop III opacities are more complex than in the analytical model
 - Mass and thickness of the radiative layer can't be neglected

$$\frac{M_{Rad}}{M_*} \approx 0.2 \quad \frac{R_{Rad}}{R_*} \approx 0.7$$

=> Upgrading to an numerical model



Numerical model

- Assume the Quasi-star as a static and spherically symmetric object
 - Equation of hydrostatic equilibrium (I.)
 - Equation of enclosed mass (II.)
 - Equation of state (III.)
 - Equation of the temperature gradient (IV.)
- To solve this system by integration
 - T_{ph}, α and M_{BH} are constant
 - Guess the photospheric radius R_* and the Quasi-star mass M_*

$$(I.) \frac{dp}{dr} = \frac{-G M(r) \rho}{r^2}$$

$$(II.) \frac{dM}{dr} = 4 \pi \rho r^2$$

$$(III.) p = p_g + p_r = \frac{\rho k T}{\mu} + \frac{1}{3} a T^4$$

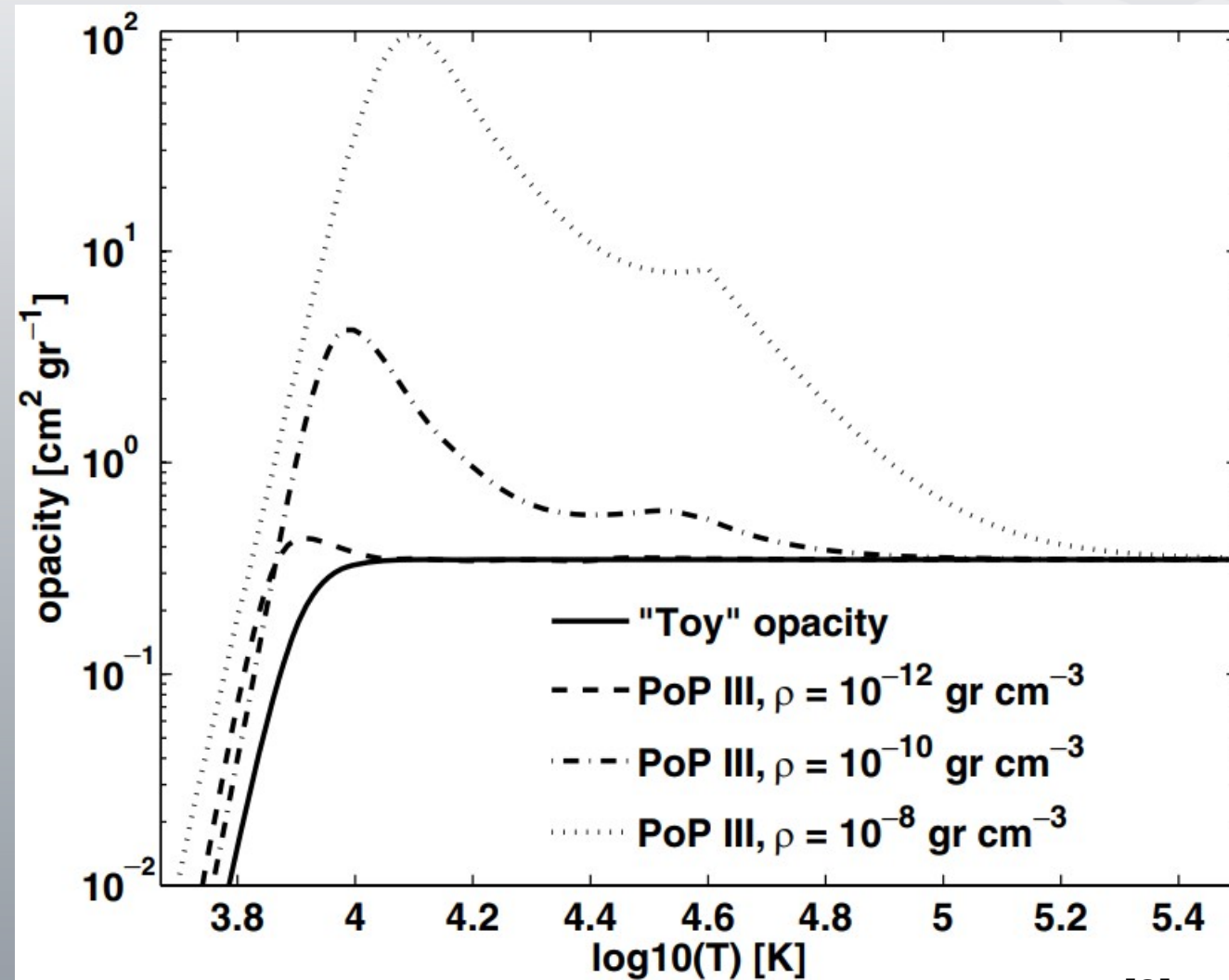
$$(IV.) \frac{dT}{dr} = \frac{dT_{rad}}{dr} - \frac{\min\left(\frac{-dT_{rad}}{dr}, \frac{-dT_{ad}}{dr}\right) + \frac{dT_{rad}}{dr}}{1 + x^{10}}$$

=> Still have to determine the quasi stars opacity

$$F_{con_{max}} = \beta c_s p_r = 0.1 \sqrt{\frac{p}{\rho}} p_r \quad x = \frac{F}{F_{con, max}}$$

Numerical model

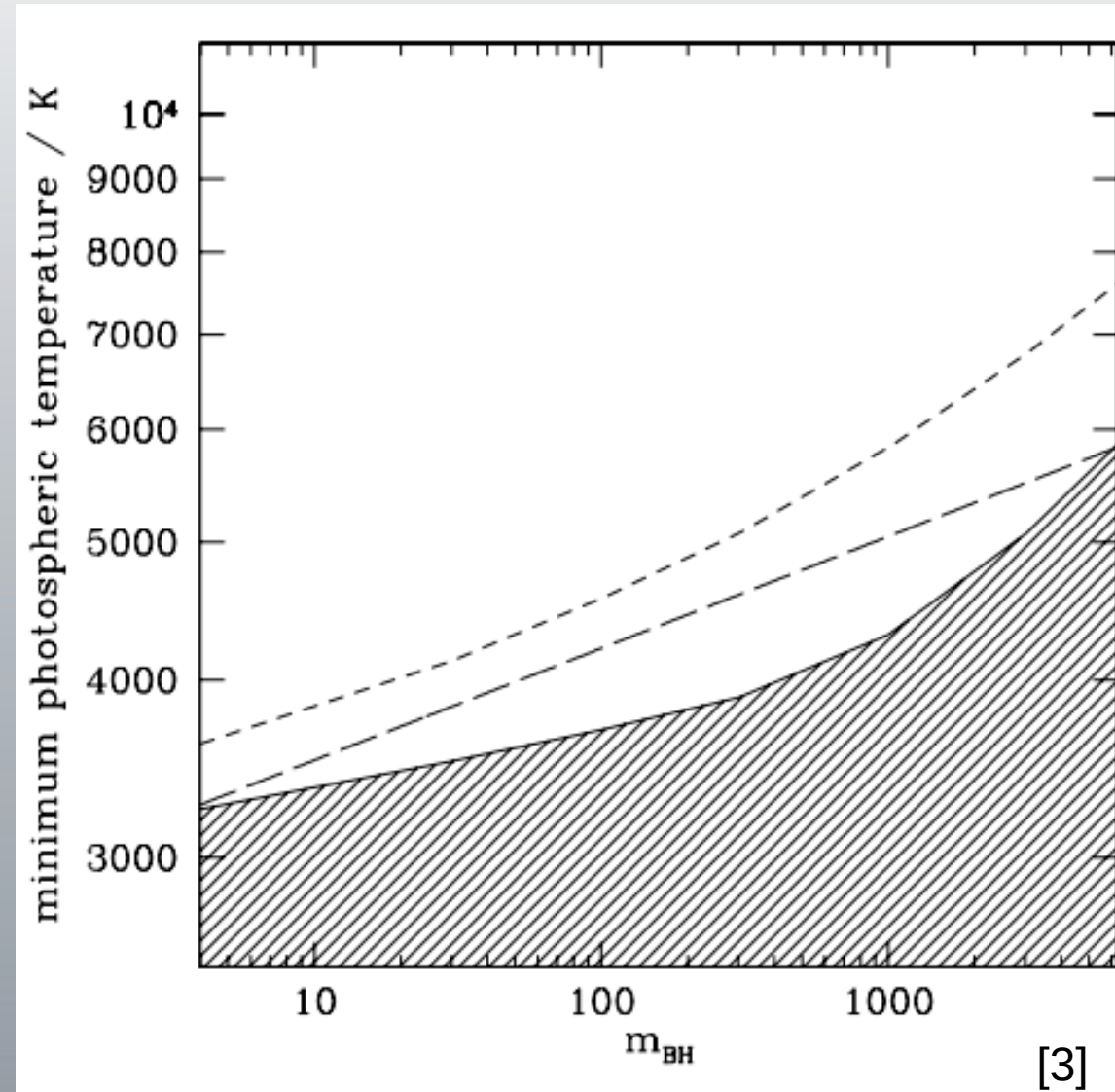
- “Toy model“ or analytic model
 - Ignores density dependence
 - Reasonable approximation
 - At low density
 - Very poor at higher density and at floor value (10^4K)
- Pop III opacity (MD05)
 - Opacity increases with over the analytic fit at increasing density
 - Bound–free peak at $T = 10^4\text{ K}$
 - Due to hydrogen ionization
 - Much better option



[3]

Numerical model

- Again a minimal T_{ph} can be found at a given α and M_{BH}
- Ensuring sub-Eddington luminosity at the transition radius
- Numerical models with the “Toy” opacity (short-dashed line)
- Analytic estimate (long-dashed line)
- Combining both analytic estimates
- Pop III opacity (solid line)
- Static quasi-star models do not exist under this line

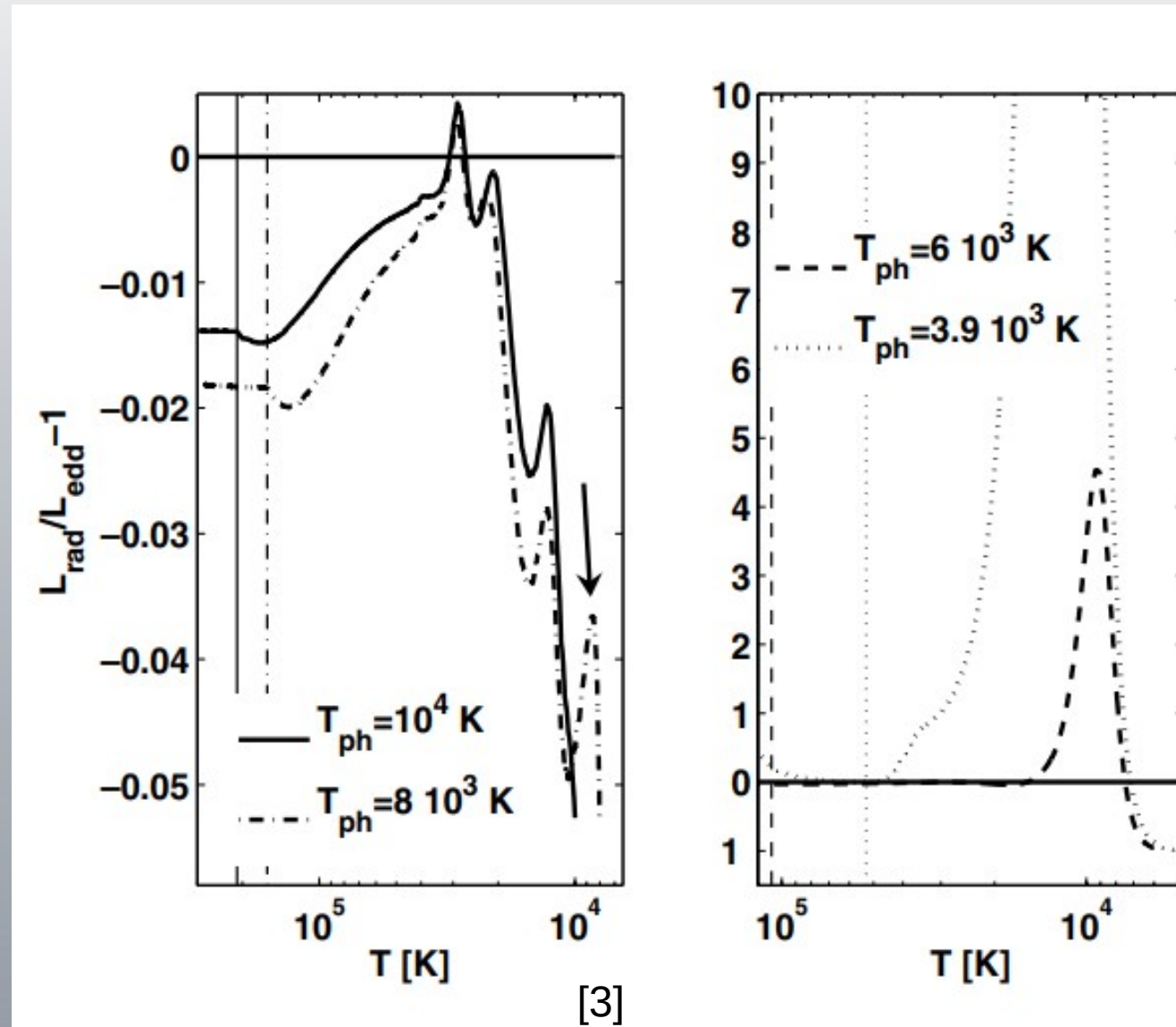


Numerical model

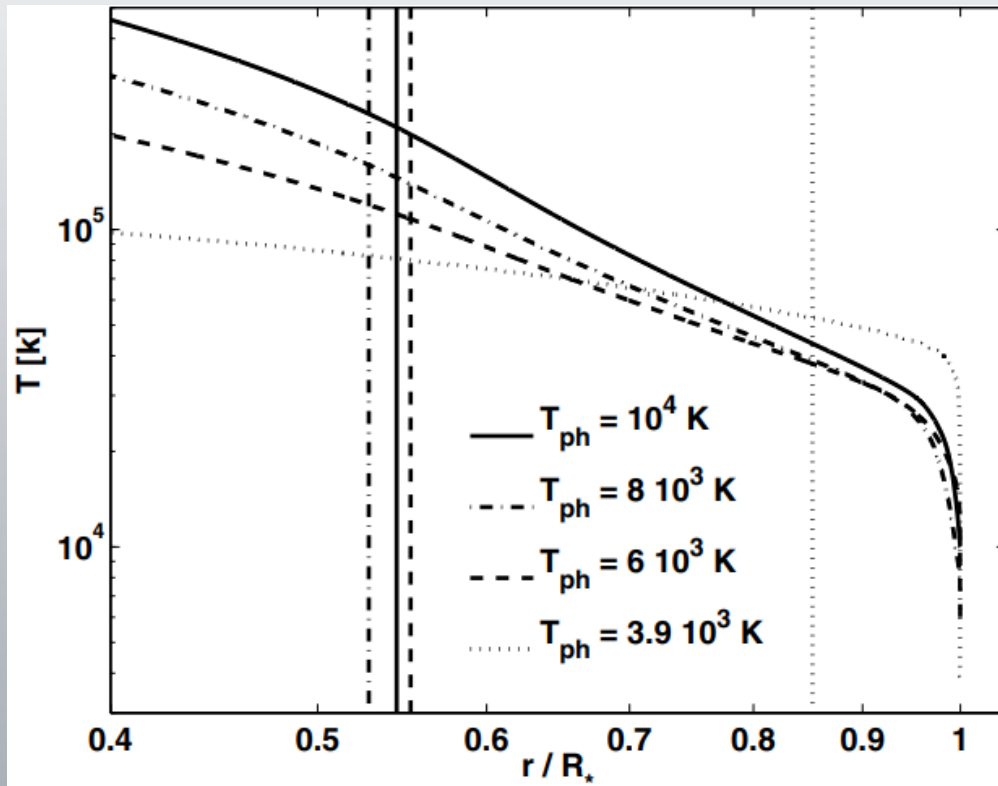
- Local Eddington ratio at a constant black hole mass
- Focusing on the radiative zone
- Some super-Eddington peaks
 - For decreasing T_{ph} at the Bound-free peak ($T = 10^4$ K)
- Narrow peak at $T = 3 \cdot 10^4$ K
- For only $T_{\text{ph}} \approx 4000$ K

=> There are still local super-Eddington fluxes for $T_{\text{ph}} > T_{\text{min}}$

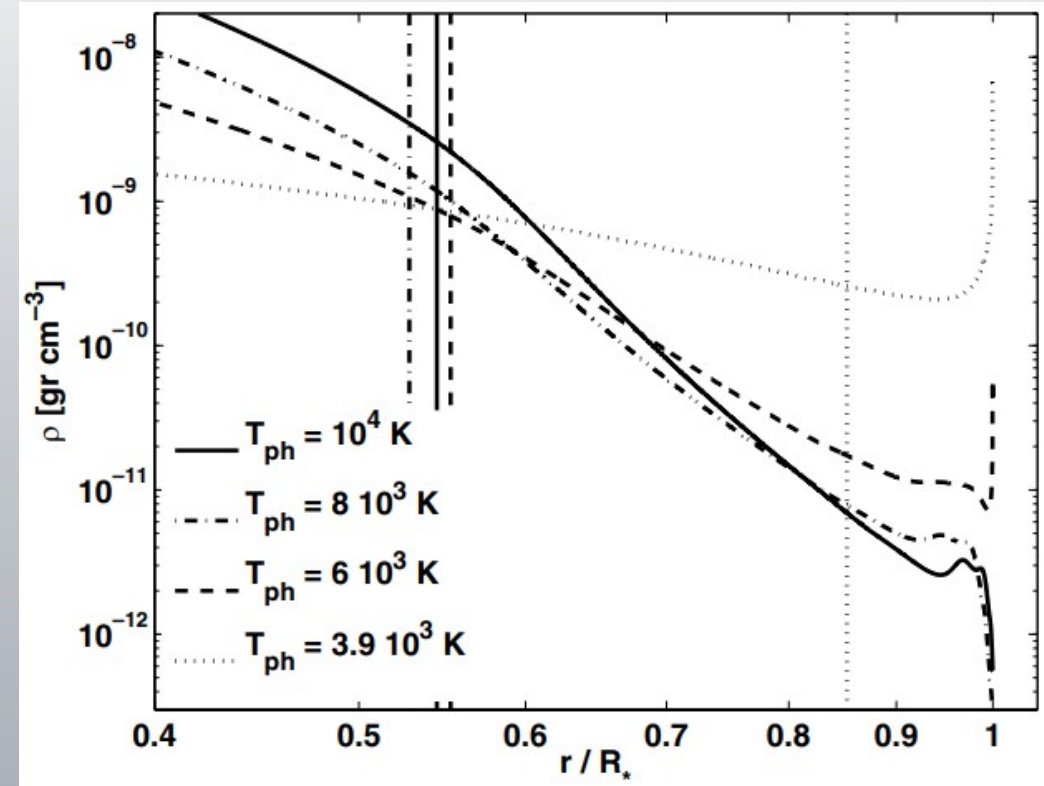
=> How does this effect our star ?



Numerical model



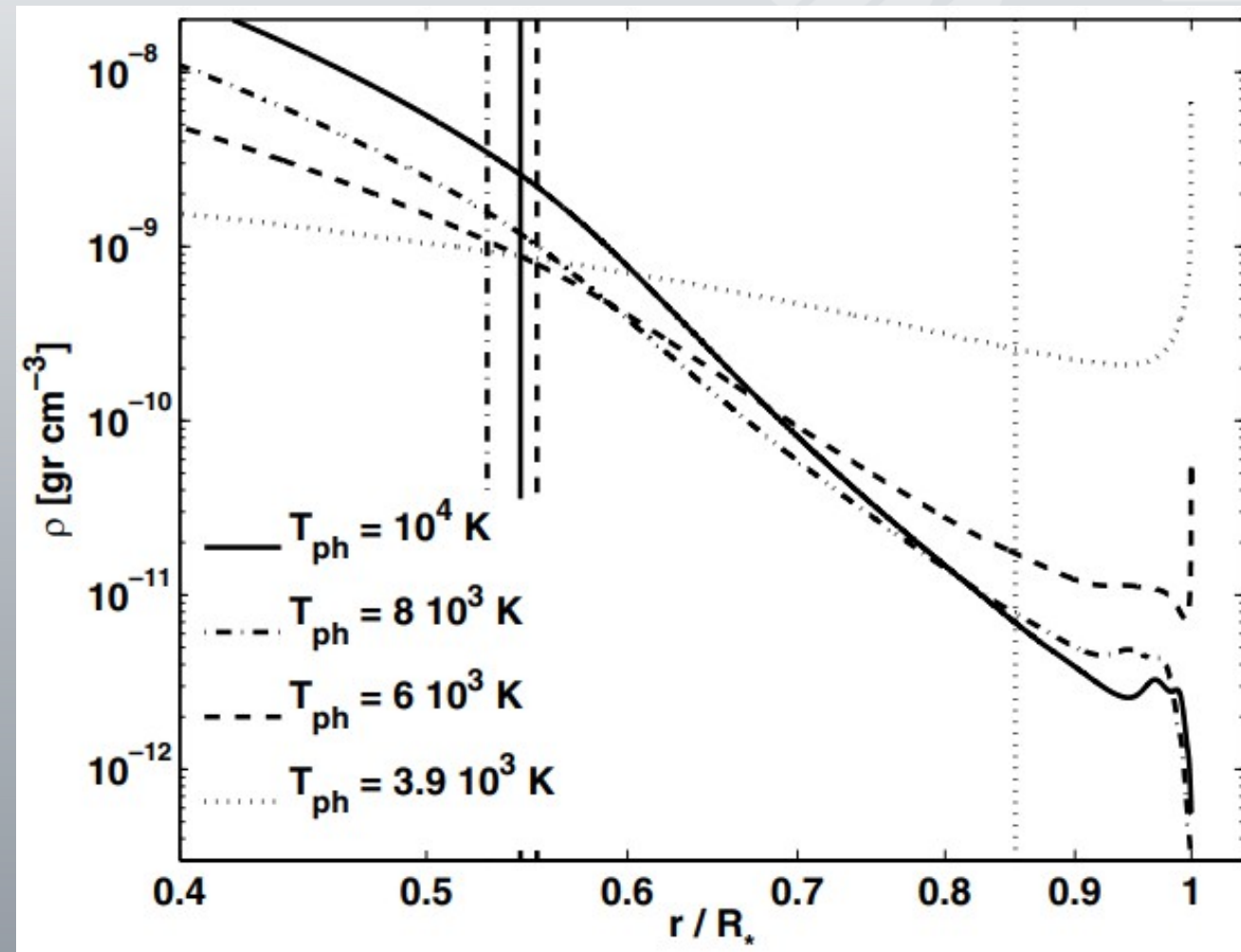
- Radial profiles of temperature and density of earlier models
- Local density inversion forms
- Meaning the density gradient becomes positive there



- => Radiative force substantially exceeds the gravitational force
- => At the same time, the temperature gradient steepens

Numerical model

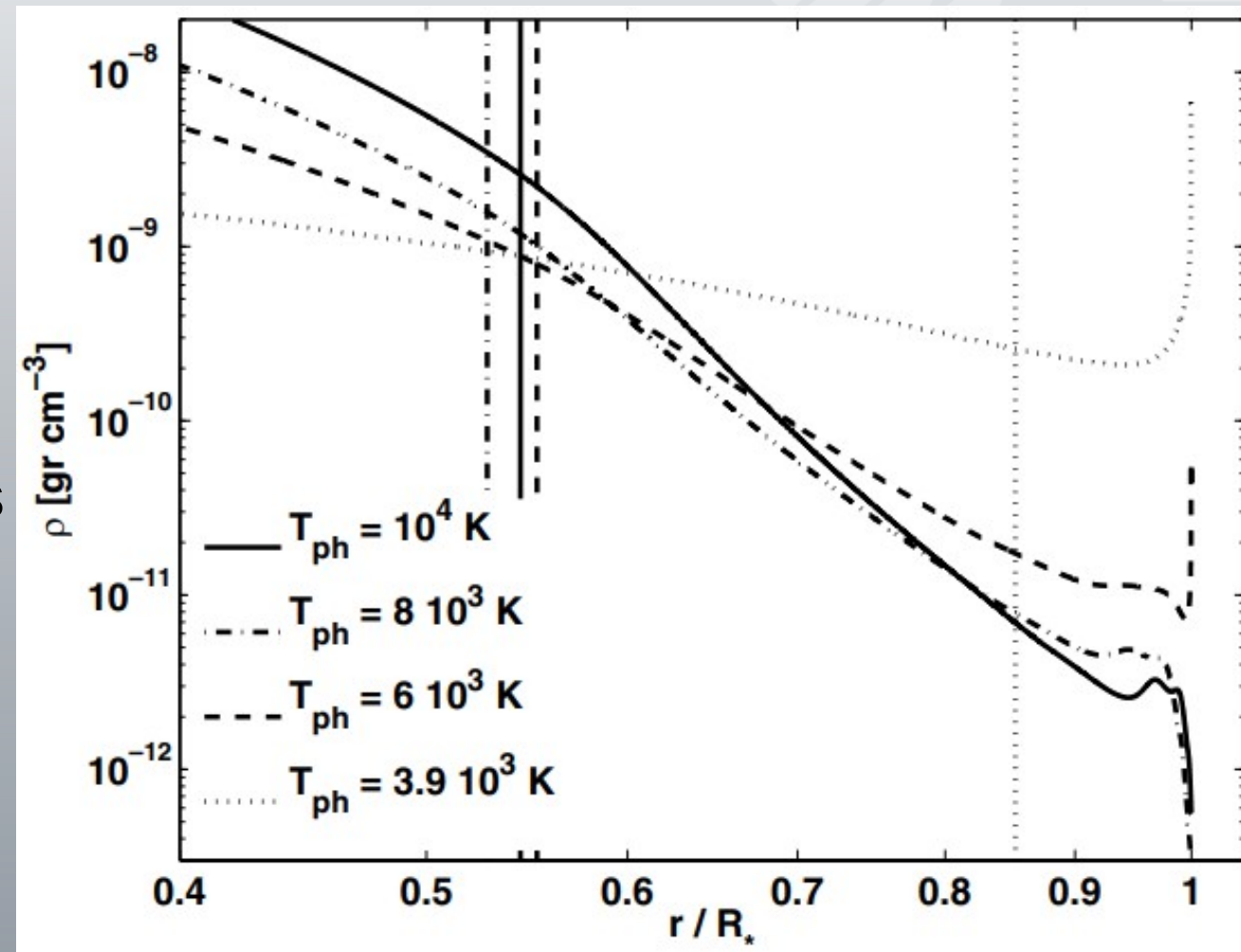
- Existence of density inversions could make the system unstable
 - It's very complicated to estimate the mass-loss rate
 - Many possible outcomes
 - Presuming for these zones
 - Creation large-scale circulation
 - Not dissimilar to convection
 - With little or no mass-loss
- => We adopt T_{\min} as an estimate for the minimum temperature a quasi-star can sustain



Numerical model

- Numerical model
- Confirms the existence of a minimum temperature at which the quasi star is stable
- Numerical integration reveals the existence of narrow regions with locally super-Eddington fluxes
 - Creating local density inversions
 - With complex and unsure behaviour

=> Look at the co-evolution model to find the final mass of the BH



Co-Evolution

- Model the co-evolution of the BH and envelope as a series of equilibrium model
 - Short thermal time-scale allows quasi-static changes
 - BH growth is confined by the Eddington limit at $T_{\text{ph}} > T_{\text{min}}$ (I.)
- Analytic Co-Evolution model
 - Constant quasi-star accretion rate at $0.1 \dot{m}_{0.1} M_{\odot} \text{yr}^{-1}$ (I.)
 - Analytic estimates for the
 - Quasi-star mass (II.)
 - Black hole mass (III.)

$$(I.) \dot{m}_{BH} = 2.5 \cdot 10^{-8} \epsilon_{0.1}^{-1} m_* M_{\odot} \text{yr}^{-1}$$

$$m_{BH} = 1.2 \cdot 10^{-7} \epsilon_{0.1}^{-1} m_*^2 \dot{m}_{0.1}^{-1}$$

$$l_{tr} = \tilde{\kappa} = 1 \quad \epsilon = \text{accretion efficiency}$$

$$(II.) m_{*,0} = 1.8 \times 10^5 \epsilon_{0.1}^{8/9} m_{0.1}^{-8/9} \alpha_{0.1}^{-4/9} T_{m,4}^{-20/9}$$

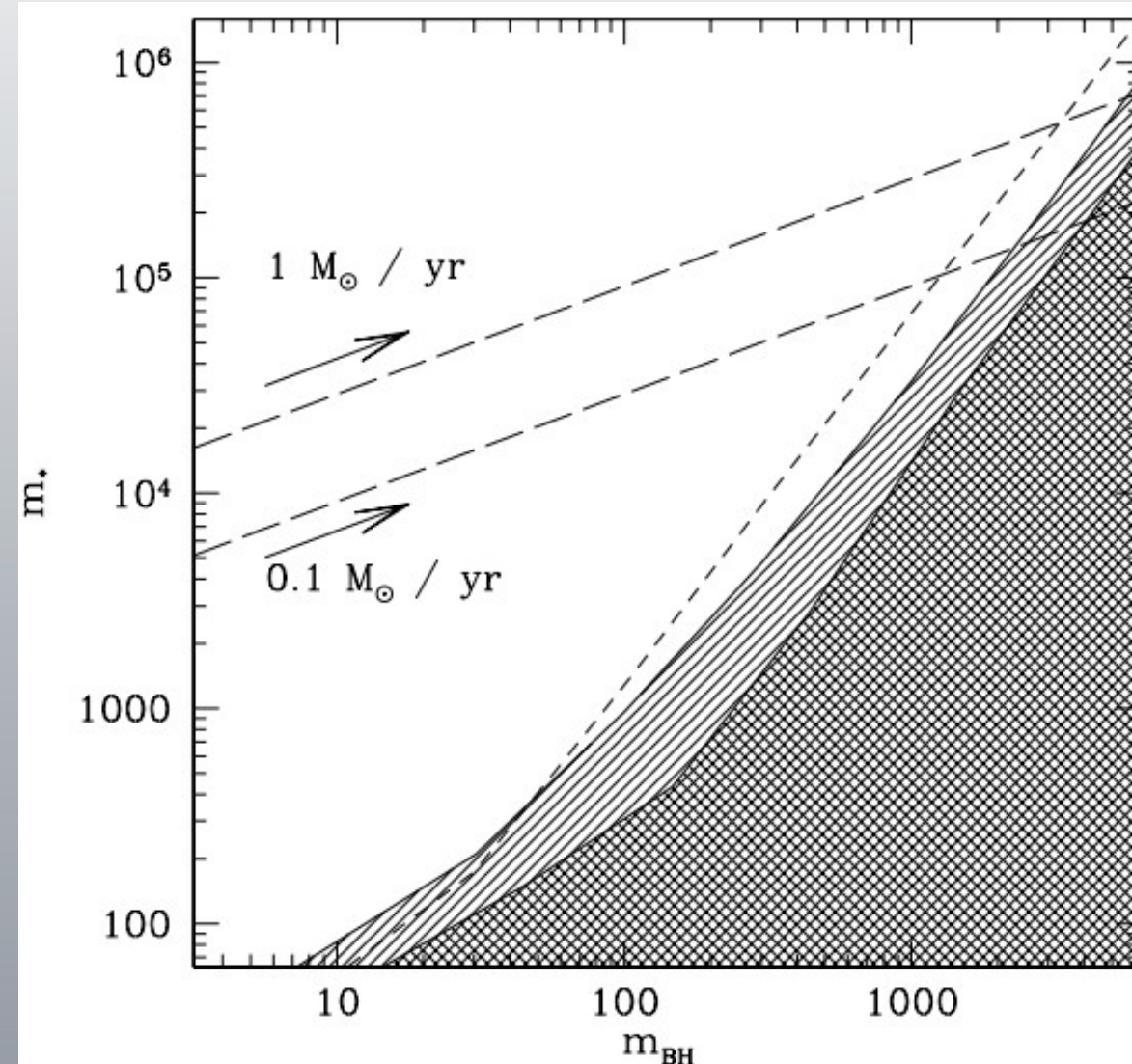
$$(III.) m_{BH,0} = 3.9 \cdot 10^3 \epsilon_{0.1}^{7/9} m_{0.1}^{-7/9} \alpha_{0.1}^{-8/9} T_{m,4}^{-40/9}$$

Co-Evolution

- To check these analytic results
- Numerically solve this set of equations while using
 - The analytic steady growth track (I.)
 - The numerically computed $T_{\min,ph}$

$$\frac{dM_*}{dt} = \dot{M}_*$$

$$\frac{dM_{BH}}{dt} = \frac{L_{BH}(M_*, M_{BH}, \alpha)}{\epsilon c^2}$$

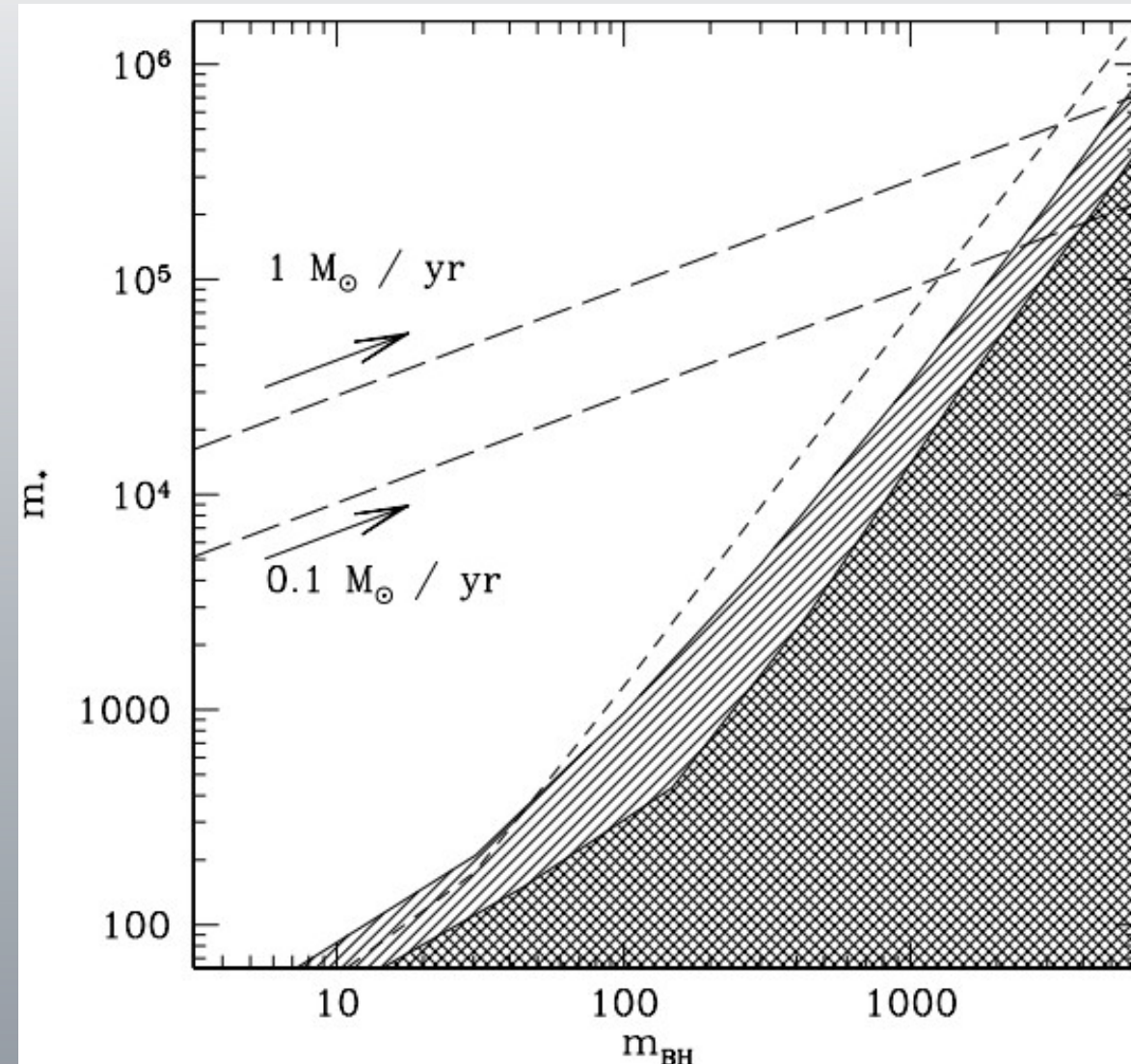


Co-Evolution

- Envelope mass versus BH mass at the minimum photospheric temperature
- Two growth tracks
- Short dashed line is the 'toy' opacity
- Solid lines are numerical opacities
- Lighter shaded region is for $\alpha = 0.1$
- Darker shaded region is for $\alpha = 0.05$

=> Final M_{BH} is higher for higher accretion rates on to the envelope and lower parameters α

=> Final M_{BH} is predicted to be at least a few thousand solar masses

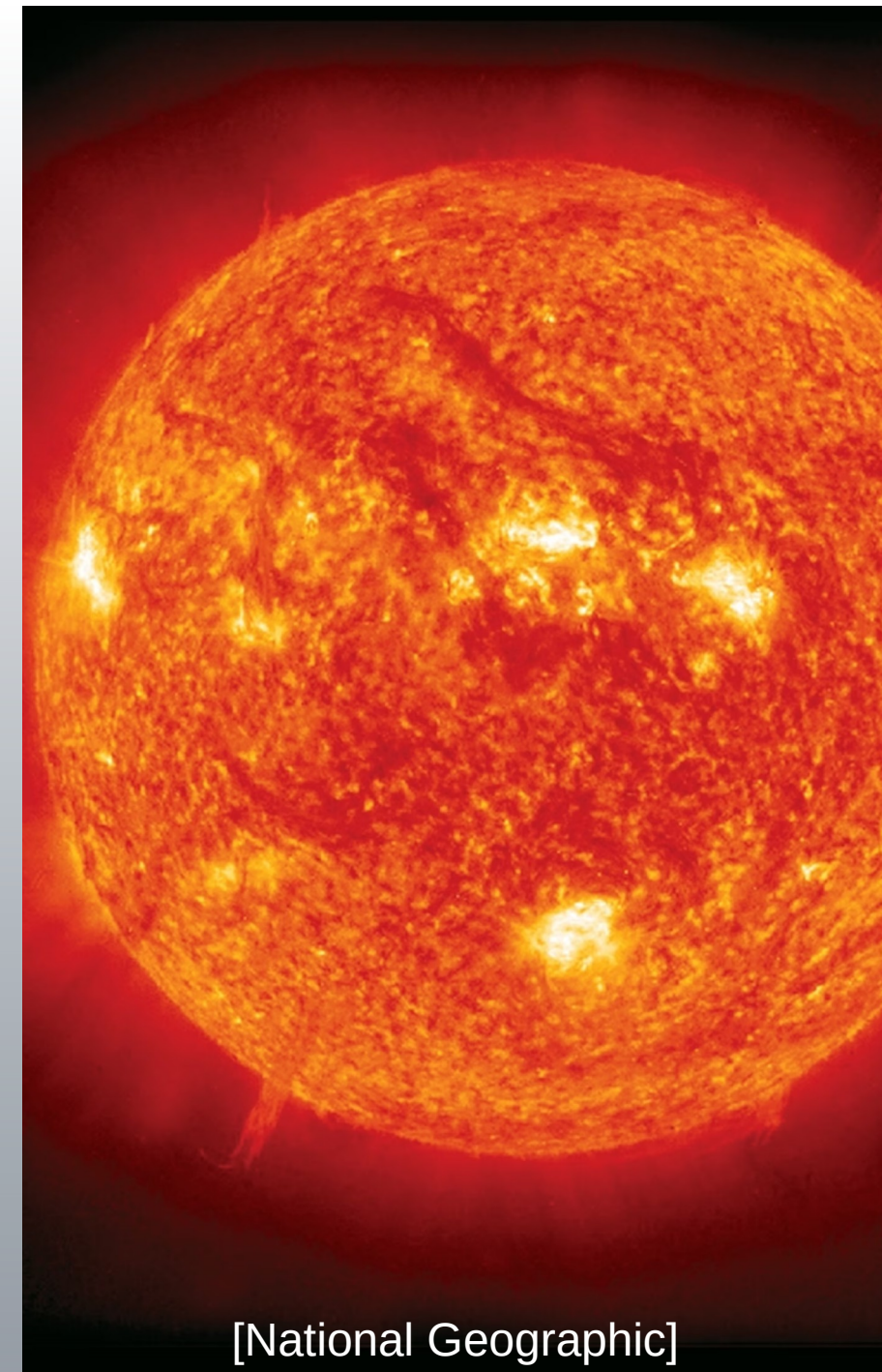


Conclusion

- Theoretical model of a quasi-star
 - Contains some uncertainties in its simplifications as well as its assumptions
 - Analytic and numerical model
 - Show the existence of a minimum photospheric temperature of around 4000 – 5000 K
 - Show that the creation of seed black holes at about a few 10^3 - $10^4 M_{\odot}$ is possible

=> Possible solution for SMBH problem

=> Have to wait for experimental evidence
(or a better theory)



[National Geographic]

Sources

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- [3] Mitchell C. Begelman, Elena M. Rossi, Philip J. Armitage, Quasi-stars: accreting black holes inside massive envelopes, Monthly Notices of the Royal Astronomical Society, Volume 387, Issue 4, July 2008, Pages 1649–1659, <https://doi.org/10.1111/j.1365-2966.2008.13344.x>
- [5] "APOD: 2023 November 10 - UHZ1: Distant Galaxy and Black Hole". apod.nasa.gov. Retrieved 2024-9-3
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- [7] Michael Mayer, Wolfgang J. Duschl, Rosseland and Planck mean opacities for primordial matter, Monthly Notices of the Royal Astronomical Society, Volume 358, Issue 2, April 2005, Pages 614–631, <https://doi.org/10.1111/j.1365-2966.2005.08826.x>

Thank you for
Your Attention!



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